

## General parameters:

$$f_0 := 2.9985 \cdot 10^9$$

$$w_0 := 2 \cdot \pi \cdot f_0$$

$$k := 1$$

Field to power  
proportionality  
constant

$$\Delta t_{out\_p} := 0.65 \cdot 10^{-6}$$

$$t_1 := 3.85 \cdot 10^{-6}$$

$$t_2 := t_1 + \Delta t_{out\_p}$$

$$t_2 = 4.5 \cdot 10^{-6}$$

$$Q_{0\_final} := 144 \cdot 10^3$$

$$\beta_{final} := 7.3$$

## Coupling factor:

$$B = Q_0 / Q_e = P_{em} / P_c$$

$$\beta := 0.1, 0.2 \dots 20$$

$$Q_L(\beta, Q_0) := \frac{Q_0}{1 + \beta}$$

## Loaded cavity time constant (Tc) and steady-state emitted field (L):

$$T_c = 2 + Q_L / w$$

$$L = 2 \cdot B / (1 + B)$$

$$T_c(\beta, Q_0) := 2 \cdot \frac{Q_L(\beta, Q_0)}{w_0}$$

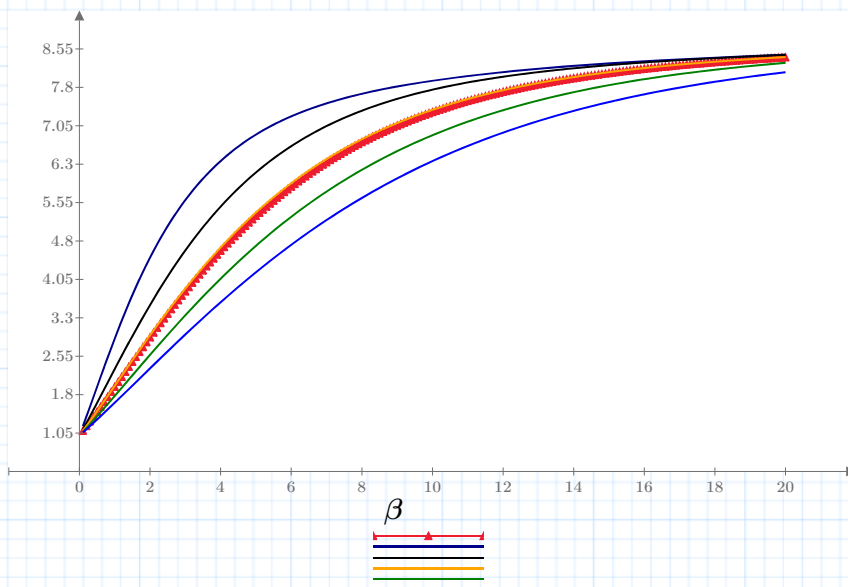
$$\alpha(\beta) := 2 \cdot \frac{\beta}{1 + \beta}$$

## Field calculation:

$$E_{max}(\beta, Q_0) := \alpha(\beta) \cdot \left( 1 - \exp\left(\frac{-t_1}{T_c(\beta, Q_0)}\right) \right) + 1$$

$$P_{max}(\beta, Q_0) := k \cdot E_{max}(\beta, Q_0)^2$$

$$Q_{0m} := \begin{bmatrix} 0.6 \cdot 10^5 \\ 0.8 \cdot 10^5 \\ 1 \cdot 10^5 \\ 1.2 \cdot 10^5 \\ 1.4 \cdot 10^5 \\ 1.6 \cdot 10^5 \\ 1.8 \cdot 10^5 \\ 2 \cdot 10^5 \\ 2.2 \cdot 10^5 \\ 2.4 \cdot 10^5 \\ 2.6 \cdot 10^5 \end{bmatrix}$$



$$P_{max}(\beta, Q_{0\_final})$$

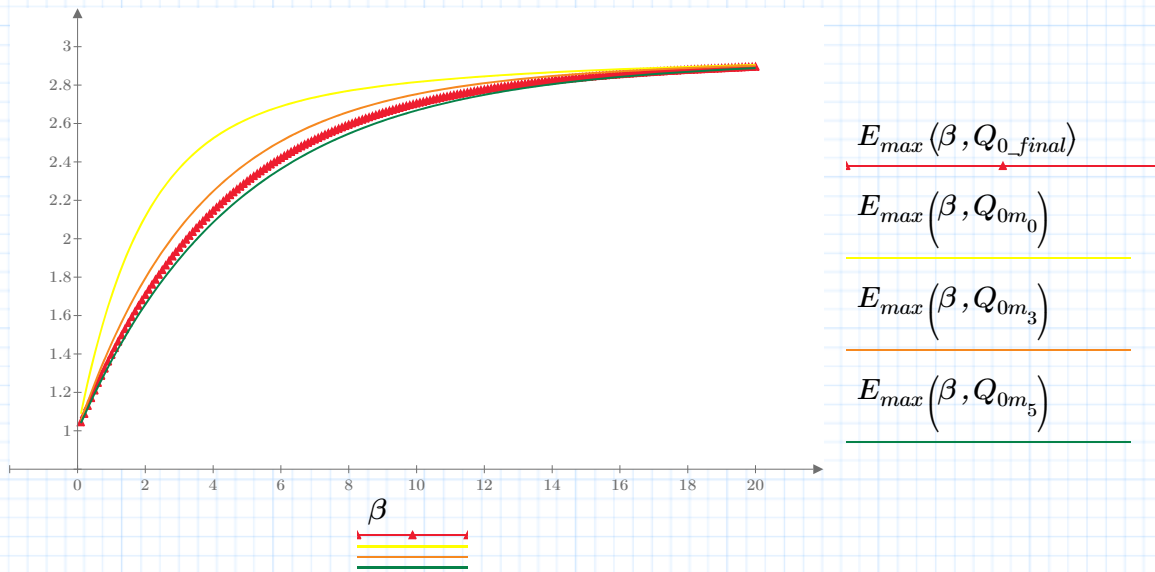
$$P_{max}(\beta, Q_{0m_0})$$

$$P_{max}(\beta, Q_{0m_2})$$

$$P_{max}(\beta, Q_{0m_4})$$

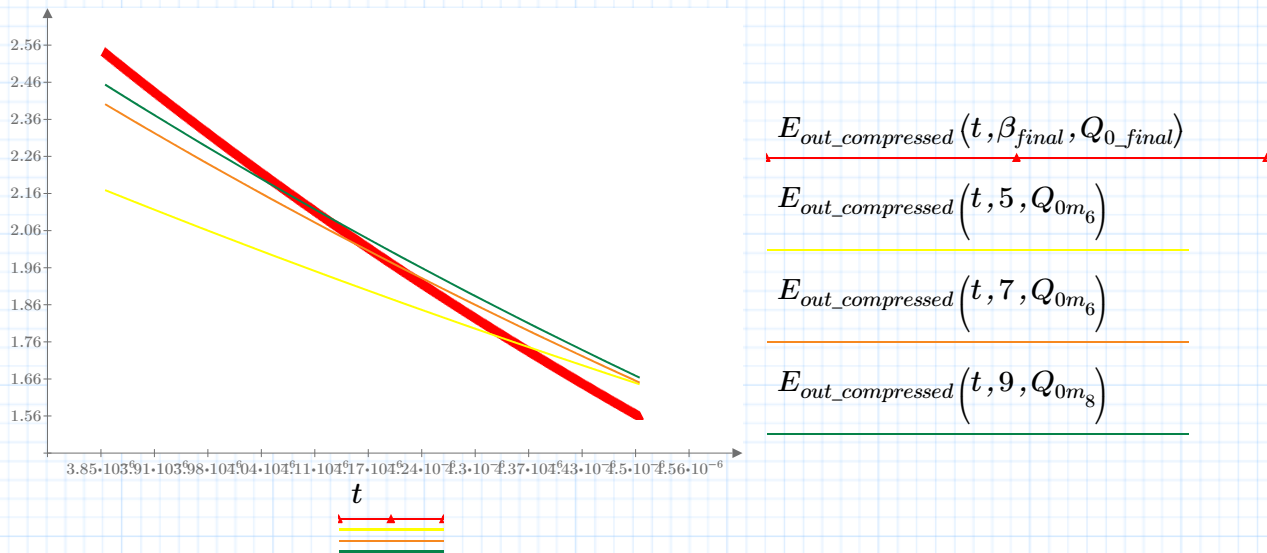
$$P_{max}(\beta, Q_{0m_6})$$

$$P_{max}(\beta, Q_{0m_8})$$



### Compressed pulse energy calculation:

$$E_{out\_compressed}(t, \beta, Q_0) := \alpha(\beta) \cdot \left( \left( 2 - \exp\left(\frac{-t_1}{T_c(\beta, Q_0)}\right) \right) \exp\left(\frac{-(t-t_1)}{T_c(\beta, Q_0)}\right) - 1 \right) + 1$$



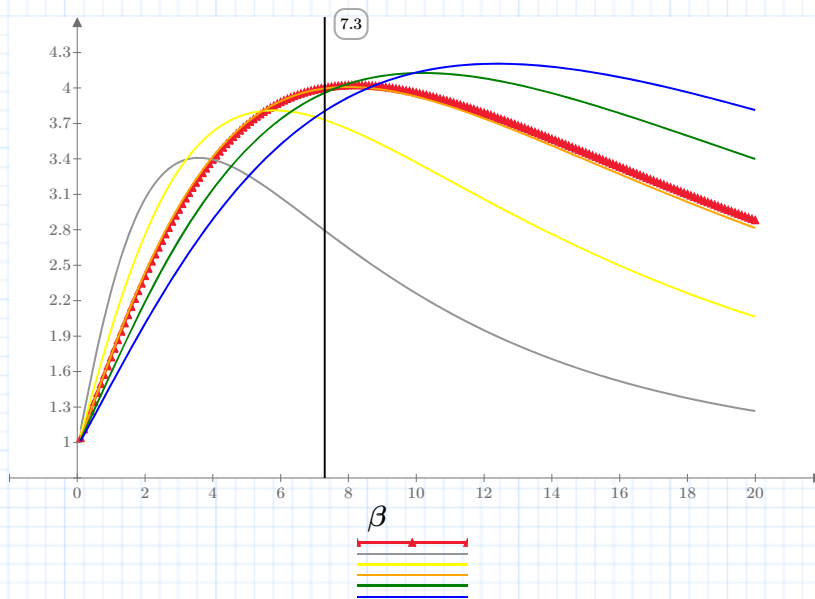
$$\xi(\beta, Q_0) := \int_{t_1}^{t_2} (E_{out\_compressed}(t, \beta, Q_0))^2 dt$$

$$\eta_{eff\_phaseflip} := 0.96$$

$$\xi_{out\_pulse\_avg}(\beta, Q_0) := \frac{\xi(\beta, Q_0)}{\Delta t_{out\_p}} \cdot \eta_{eff\_phaseflip}$$

$$\xi_{out\_pulse\_avg}(\beta_{final}, Q_{0\_final}) = 4.002$$

## Coupling factor and Q analysis



$$\xi_{out\_pulse\_avg}(\beta, Q_{0\_final})$$

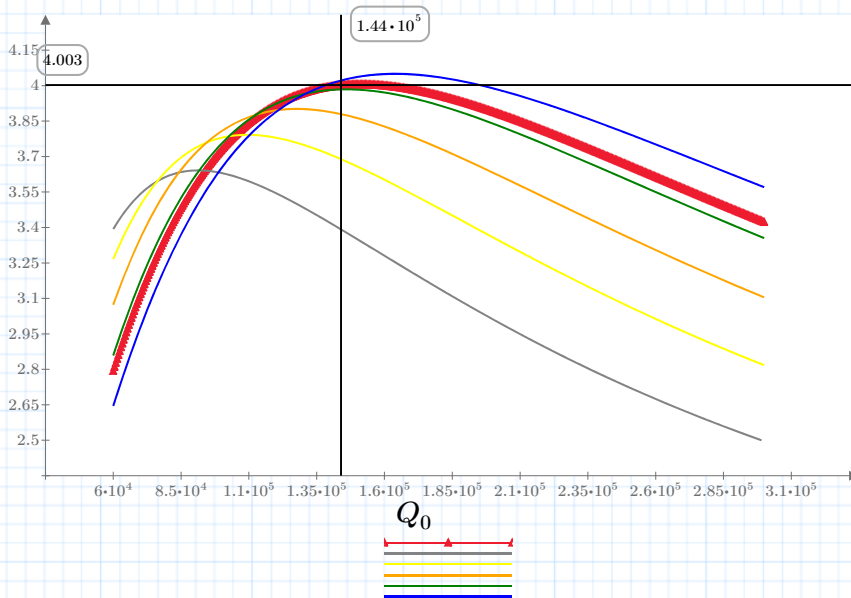
$$\xi_{out\_pulse\_avg}(\beta, Q_{0m_0})$$

$$\xi_{out\_pulse\_avg}(\beta, Q_{0m_2})$$

$$\xi_{out\_pulse\_avg}(\beta, Q_{0m_4})$$

$$\xi_{out\_pulse\_avg}(\beta, Q_{0m_6})$$

$$\xi_{out\_pulse\_avg}(\beta, Q_{0m_8})$$



$$\xi_{out\_pulse\_avg}(\beta_{final}, Q_0)$$

$$\xi_{out\_pulse\_avg}(4, Q_0)$$

$$\xi_{out\_pulse\_avg}(5, Q_0)$$

$$\xi_{out\_pulse\_avg}(6, Q_0)$$

$$\xi_{out\_pulse\_avg}(7, Q_0)$$

$$\xi_{out\_pulse\_avg}(8, Q_0)$$

## SLED in use:

### Params definition

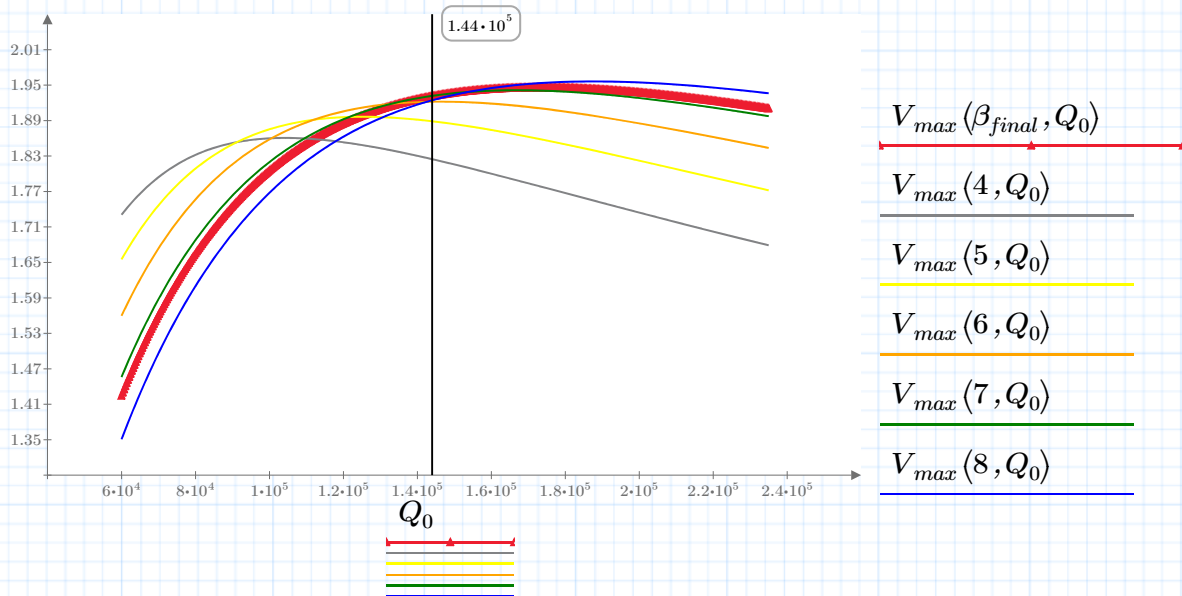
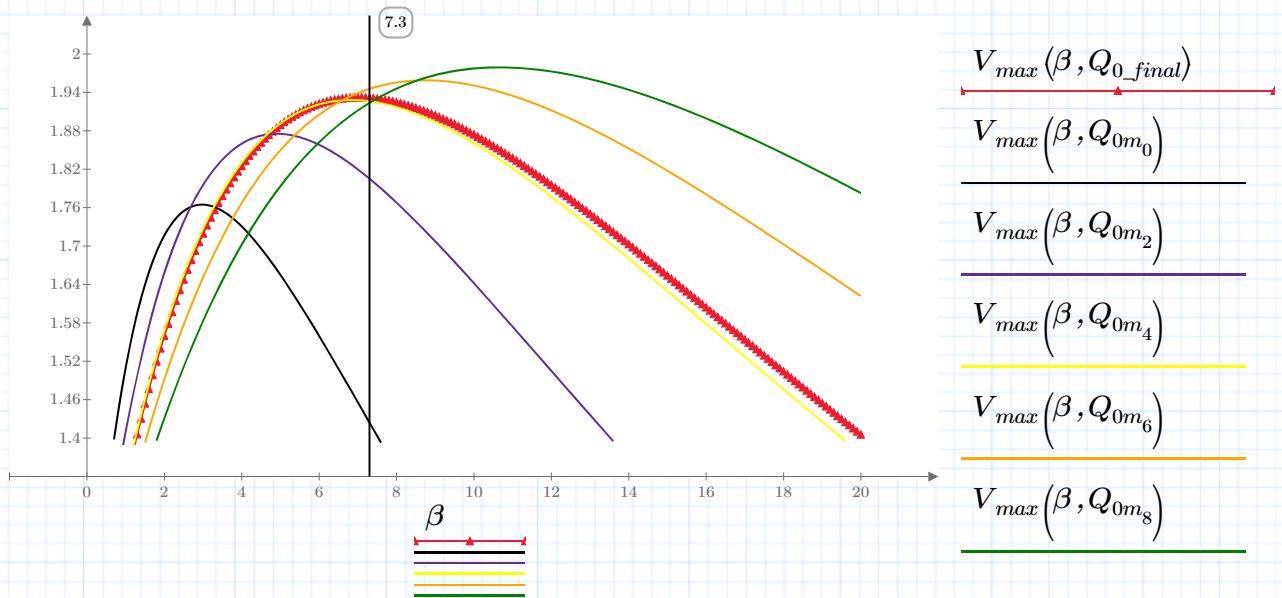
$g := 0.681$  Slope of structure group velocity

$T_f := \Delta t_{out\_p}$  Structure filling time

$$C_p(\beta, Q_0) := 1 + \frac{T_f}{T_c(\beta, Q_0) \cdot \ln(1-g)}$$

$$V_{max}(\beta, Q_0) := \frac{\alpha(\beta)}{g \cdot C_p(\beta, Q_0)} \cdot \exp\left(\frac{-T_f}{T_c(\beta, Q_0)}\right) \left(2 - \exp\left(\frac{-t_1}{T_c(\beta, Q_0)}\right)\right) \cdot \left(1 - (1-g)^{C_p(\beta, Q_0)}\right) - \alpha(\beta) + 1$$

$$V_{max}(\beta_{final}, Q_{0\_final}) = 1.931$$



### Spherical cavity dimensioning:

$$Q_{0\_opt} := 1.8 \cdot 10^5$$

$$\delta_{Cu}(f) := \frac{0.066}{\sqrt{f}}$$

skin effect of copper

$$\delta_{Cu\_f0} := \delta_{Cu}(f_0)$$

$$\delta_{Cu\_f0} = 1.205 \cdot 10^{-6}$$

1.195 @ 3 GHz according to other sources

$$a := Q_{0\_opt} \cdot \delta_{Cu\_f0} \cdot m = 0.217 \text{ m}$$

sphere radius

$$u_{np} := 14.066$$

$$f_{res} := \frac{u_{np}}{2 \cdot \pi \cdot a \cdot \sqrt{\epsilon_0 \cdot \mu_0}} = (3.093 \cdot 10^9) \frac{1}{m} \cdot \frac{m}{s}$$